



Progression in Calculations (2022/23)

"Mathematics is a creative and highly inter-connected discipline that has been developed over centuries, providing the solution to some of history's most intriguing problems. It is essential to everyday life, critical to science, technology and engineering, and necessary for financial literacy and most forms of employment. A high-quality mathematics education therefore provides a foundation for understanding the world, the ability to reason mathematically, an appreciation of the beauty and power of mathematics, and a sense of enjoyment and curiosity about the subject."

National Curriculum in England 2014

Department for Education

This calculation policy is a guide for all staff at Ludlow Primary School and forms part of the mathematics policy.

It is designed to be used alongside any teaching resources that teachers wish to use.

All staff have access to Maths-No Problem resources which provides lessons and a host of ideas and activities to develop mastery in Mathematics. These resources are excellent ways to support the learning of mathematics and should be tailored to support the needs of the pupils. Staff are also encouraged to access the NCETM and White Rose Websites for further ideas and guidance. In EYFS, Development Matters statements are referred to; to inform planning and progress towards meeting the Early Learning Goals:

All teachers have access to the schemes of work from the White Rose Maths Hub. This module also uses the Singapore Maths Methods and is affiliated to the workings of the New Mathematics Curriculum that is running throughout the school. Where appropriate, staff are encouraged to base their planning around these recommended modules. However, it should be emphasised that all planning should take account of the requirements of the pupils in terms of where they are in their learning and how they can achieve successful outcomes. Teachers are responsible for making these judgements.

The White Rose Maths schemes of work provide sequential programmes of study that are underpinned by promoting fluency in number. They emphasise that all pupils must have a thorough grounding in the four basic rules of number before progressing on to the next level. This complete understanding gives pupils more confidence in dealing with number activities and in turn, leads to mastery of the four operations.

Whilst the calculation policy guidance document is separated into year group phases, these are intended to be used only as a guide and it is the teachers' professional judgement as to when the pupils move on to the next phase.



Progression in Calculations (2022/23)

	EYFS	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
A d d i t i o n	Saying which number is one more than a given number. Finding the total number of items in two groups by counting all of them. Finding the total by starting at the bigger number and counting on. Introduce the part part whole model.	Combining two parts to make a whole: part whole model. Starting at the bigger number and counting on. Regrouping to make 10.	Adding three single digits. Column method – no regrouping.	Column method – regrouping. (Up to 3 digits)	Column method – regrouping. (Up to 4 digits)	Column method – regrouping. (with more than 4 digits) Decimals – with the same amount of decimal places	Column method – regrouping. Decimals – with the different amounts of decimal places
S u b t r a c t i o n	Taking away using objects or drawing and crossing out. Saying which number is one less than a given number. Subtracting two single digit numbers by counting back. Introduce the part part whole model.	Taking away ones Counting back Find the difference Part part whole model Make 10	Counting back Finding the difference Part whole model Make 10 Column method – no regrouping	Column method – regrouping. (Up to 3 digits)	Column method – regrouping. (Up to 4 digits)	Column method – regrouping. (with more than 4 digits) Decimals – with the same amount of decimal places	Column method – regrouping. Decimals – with the different amounts of decimal places
M u l t i p l i c a t i o n	Problem solving - doubling	Doubling Counting in multiples	Doubling Counting in multiples Repeated addition Arrays – showing commutative multiplication	Counting in multiples Repeated addition Arrays – showing commutative multiplication	Column multiplication (2 and 3 digit multiplied by 1 digit)	Column multiplication (up to 4 digit numbers multiplied by 1 or 2 digits)	Column multiplication (multi digit numbers multiplied by a 2 digit number). Including multiplying decimals
D i v i s i o n	Problem solving – halving and sharing.	Sharing objects into groups Division as grouping	Division as grouping Division within arrays	Division within arrays Division with a remainder Short Division (2 digits by 1 digit- concrete and pictorial)	Division within arrays Division with a remainder Short Division (up to 3 digits by 1 digit- concrete and pictorial)	Short Division (up to 4 digits by a 1 digit number interpret remainders appropriately for the context)	Short division Long division (up to 4 digits by a 2 digit number interpret remainders as whole numbers, fractions as required)

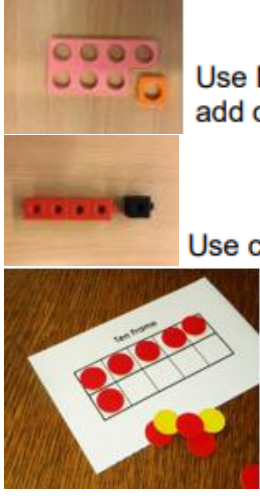





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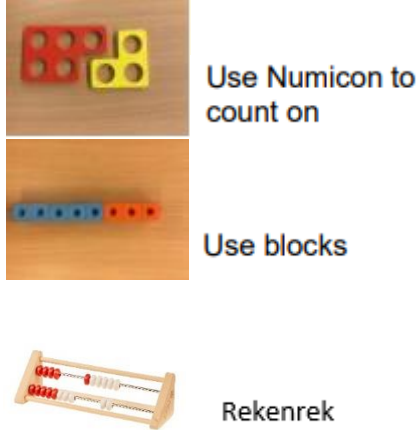

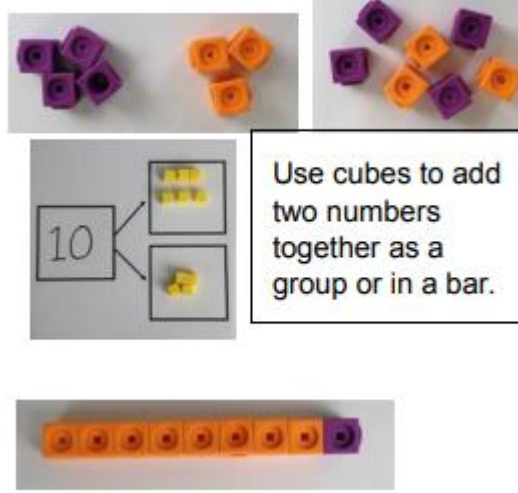
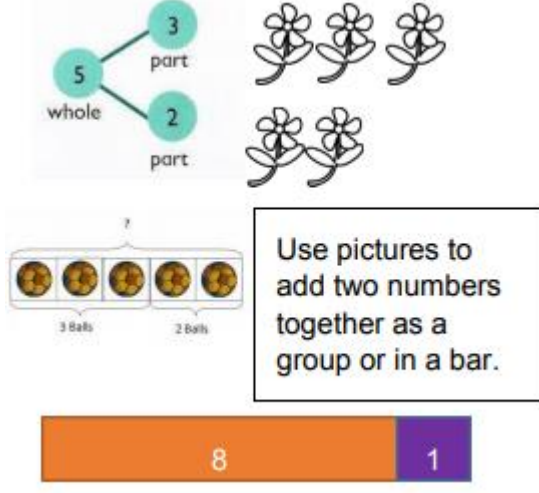

Addition Vocabulary

Year R	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
More One more More than Add Addition Equals Total Make Plus Part Whole Altogether And Number bonds	Number bonds Represents Sign Subitize Counting on Commutative Systematic Greater than	Column addition Column method Exchange Regroup Estimate Inverse	Regroup Increase Operation	Commutative Sum Integer	Equal to Is the same as	Annexing Vertical Algorithm

Addition progression

Objectives and strategies	Concrete	Pictorial	Abstract
<p>Saying which number is more than a given number</p>	 <p>Use Numicon to add one more</p> <p>Use cubes</p> <p>Ten Frame</p>	 <p>Use pictures to add one more</p>	<p>4 and 1 makes <input type="text"/></p> <p>$4 + 1 = \square$</p>
<p>Finding a total number of items in two groups by counting all</p>	 <p>Use Numicon</p> <p>Use objects</p>	 <p>Use pictures to add 2 groups</p>	<p>3 and 4 makes <input type="text"/></p> <p>$3 + 4 = \square$</p>

Progression in Calculations (2022/23)

<p>Finding the total number of items in two groups by counting on</p>	 <p>Use Numicon to count on</p> <p>Use blocks</p> <p>Rekenrek</p>	 <p>Counting on using pictures</p>	<p>$5 + 3 = \square$</p> <p>Move into abstract (holding larger numbers in head)</p>
<p>Combining two parts to make a whole: part-whole model</p>	 <p>Use cubes to add two numbers together as a group or in a bar.</p>	 <p>Use pictures to add two numbers together as a group or in a bar.</p>	<p>$4 + 3 = 7$</p> <p>$10 = 6 + 4$</p>  <p>Use the part-part whole diagram as shown above to move into the abstract.</p>

Progression in Calculations (2022/23)

Starting at the bigger number and counting on

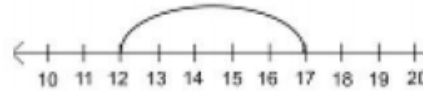


Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.



Rekenrek

$$12 + 5 = 17$$

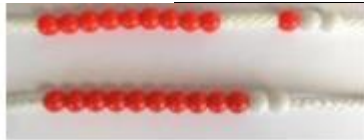


Start at the larger number on the number line and count on in ones or in one jump to find the answer.

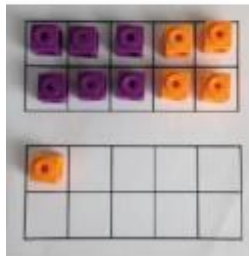
$$5 + 12 = 17$$

Place the larger number in your head and count on the smaller number to find your answer.

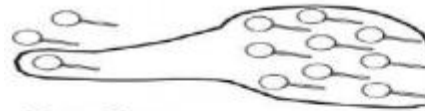
Regrouping to make 10.



$$6 + 5 = 11$$

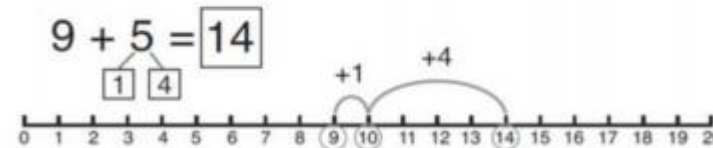


Start with the bigger number and use the smaller number to make 10.



$$3 + 9 =$$

Use pictures or a number line. Regroup or partition the smaller number to make 10.



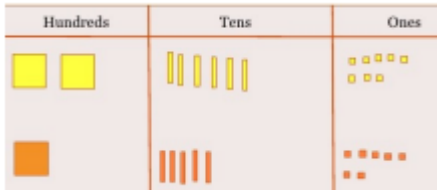
$$7 + 4 = 11$$

If I am at seven, how many more do I need to make 10. How many more do I add on now?

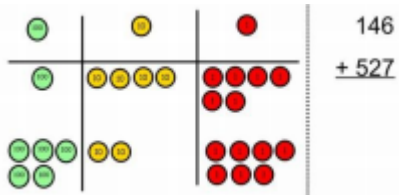
Progression in Calculations (2022/23)

Column method with regrouping

This process is to be done with the base 10 equipment to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100. Add, re-group 10 ones for a ten and 10 tens for a hundred.

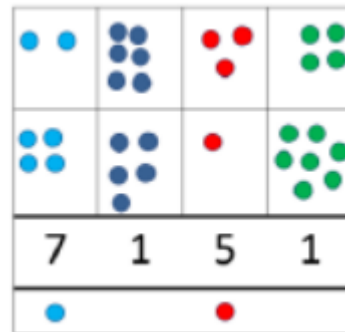
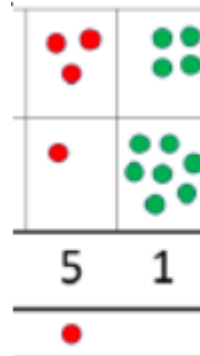


Progressing to place value counters. Make both numbers on a place value grid.



Add up the ones and re-group 10 ones for one 10.

Children draw a pictorial representation of the place value frame and counters to further support their learning and understanding re-grouping the ten underneath the equals line.



Start by partitioning the numbers before moving on to formal written methods clearly show the re-grouping.

$$25 + 48 =$$

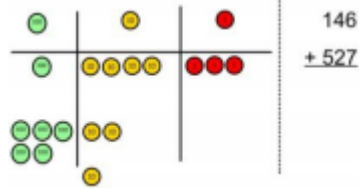
$$\begin{array}{r} 20 + 5 \\ 40 + 8 \\ \hline 60 + 13 = 73 \end{array}$$

Add the ones first, then the tens, then the hundreds.

$$\begin{array}{r} \text{HT O} \\ 536 \\ + 85 \\ \hline 621 \\ 11 \end{array}$$

As the children move on, introduce decimals with the same number of decimal

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Add up the rest of the columns, re-grouping the 10 counters from one column for the next place value column until every column has been added.

As children move on to decimals, money and decimals place value counters can be used to support learning.



places and different places. Money can be used here.

$$\begin{array}{r}
 72.8 \\
 + 54.6 \\
 \hline
 127.4
 \end{array}$$

$$\begin{array}{r}
 \text{£ } 23.59 \\
 + \text{£ } 7.55 \\
 \hline
 \text{£ } 31.14
 \end{array}$$

$$\begin{array}{r}
 81,059 \\
 3,668 \\
 15,301 \\
 + 20,551 \\
 \hline
 120,579
 \end{array}$$

Insert zeros for place holders.

$$\begin{array}{r}
 23.361 \\
 9.080 \\
 59.770 \\
 + 1.300 \\
 \hline
 93.511
 \end{array}$$







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Subtraction Vocabulary

Year R	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Fewer Subtraction Take away Less Count Back First, Then, Now How many left Minus	Difference Find the difference Difference between Smaller Less than Subitise Part Whole Partition Related facts	Column method Column subtraction Exchange Regroup Count on to find the difference	Regroup			Decomposition



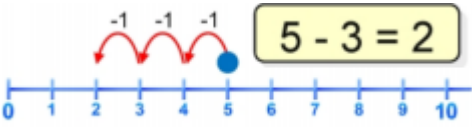
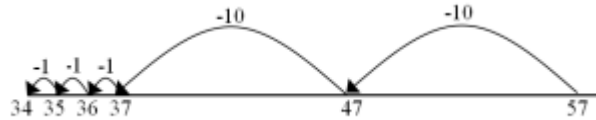
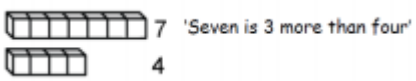
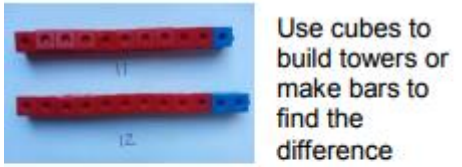
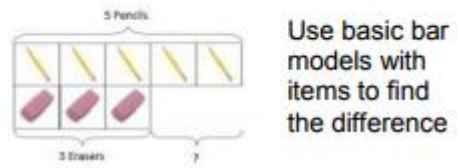
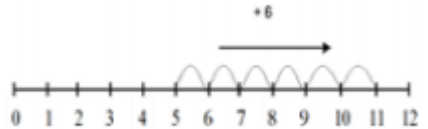
Subtraction Progression

Objectives and strategies	Concrete	Pictorial	Abstract
<p>Subtraction as take away</p>	 <p>Physically taking away</p> <p>Tractor pull</p> <p>Ten Frame</p>	 <p>Crossing out</p>	<p>4 take away 2 makes <input type="text"/></p> <p>$4 - 2 =$ <input type="text"/></p>
<p>Saying which number is one less than a given number</p>	 <p>Physically removing one item</p> <p>"Yum"</p>	 <p>Crossing out one</p>	<p>4 take away 1 makes <input type="text"/></p> <p>1 less than 4 is <input type="text"/></p> <p>1 fewer than 4 is <input type="text"/></p>

Progression in Calculations (2022/23)

<p>Subtracting two single digit numbers by counting back</p>	<p>Physical number line</p>	<p>Counting back on number line</p>	<p>$9 - 4 = \square$</p> <p>Put larger number in head and count back</p>
<p>Taking away ones</p>	<p>Use physical objects, counters, cubes etc to show how objects can be taken away.</p> <p>$6 - 4 = 2$</p> <p>Ten Frame</p>	<p>Cross out drawn objects to show what has been taken away.</p> <p>$15 - 3 = \square$</p> <p>Counting back on number line</p>	<p>$7 - 4 = 3$</p> <p>$6 = 8 - 2$</p> <p>$18 - 3 = 15$</p>

Progression in Calculations (2022/23)

<p>Counting back</p>	<p>Move objects away from the group, counting backwards.</p>  <p>Make the larger number in your subtraction. Move the beads along the bead string as you count backwards in ones.</p> 	<p>Count back in ones using a number line.</p>  <p>This can progress all the way to counting back using two 2 digit numbers.</p> 	<p>Put 13 in your head, count back 4. What number are you at?</p>
<p>Find the difference</p>	<p>Compare amounts and objects to find the difference.</p>   	<p>Count on using a number line to find the difference.</p> 	<p>Hannah has 23 sweets. Her sister has 15 sweets. Find the difference between the number of sweets.</p> <p>Ben has 12 marbles, and his brother has 5. How many more marbles does Ben have than his brother?</p>

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		<p style="text-align: center;">Comparison Bar Models</p> <p>Draw bars to find the difference between 2 numbers.</p> <p style="text-align: center;"><i>Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them.</i></p>	
<p>Part Whole Model</p>	<p>Link to addition – use the part whole model to help explain the inverse between addition and subtraction.</p> <p>If 10 is the whole and 6 is one of the parts. What is the other part?</p> <p>$10 - 6 =$</p>	<p>Use a pictorial representation of objects to show the part whole model.</p>	<p>Move to using numbers within the part whole model.</p>
<p>Make 10</p>	<p>$14 - 5$</p> <p>Make 14 on the ten frame. We will partition the 5. Take away the 4 first to make 10 and then take away 1 more so you have taken away 5.</p>	<p>Use a number line.</p> <p>$13 - 7 =$ Start at 13. Partition the 7 into a 3 and a 4 so can take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether.</p>	<p>$16 - 8 =$</p> <p>Partition the 8.</p> <p>How many do we take off to reach the next 10?</p> <p>How many do we have left to take off?</p>

Progression in Calculations (2022/23)

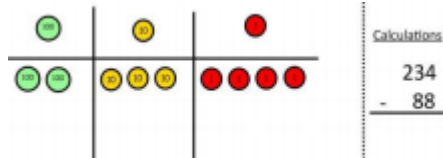
		$13 - 7 = 6$ 	
<p>Column method without regrouping</p>	<p>Use the base 10 equipment to make the bigger number then take the smaller number away.</p> <p>Show how you partition numbers to subtract. Again make the larger number first.</p>	<p>Draw the Base 10 or place value counters alongside the written calculation to support understanding.</p> <p>Calculations</p> $\begin{array}{r} 54 \\ - 22 \\ \hline 32 \end{array}$ <p>Calculations</p> $\begin{array}{r} 176 - 64 = \\ 176 \\ - 64 \\ \hline 112 \end{array}$	<p>Intermediate step of partitioning.</p> $47 - 24 = 23$ $\begin{array}{r} 40 + 7 \\ - 20 + 4 \\ \hline 20 + 3 \end{array}$ <p>This will lead to a clear written column subtraction.</p>

Progression in Calculations (2022/23)

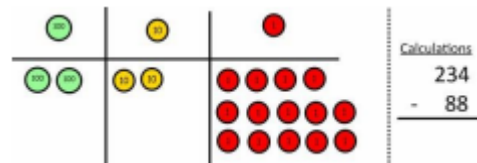
Column method with regrouping

Use Base 10 to start with before moving onto place value counters. Start with one regrouping before moving onto subtractions with 2 regroupings then onto 3.

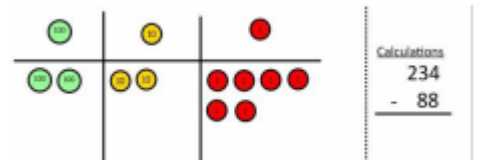
Make the larger number with the place value counters



Start with the ones, can I take 8 from 4? I need to regroup one of my tens for 10 ones.

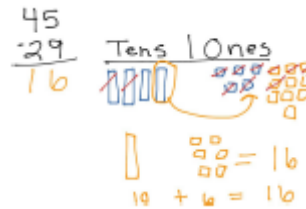


Now I can subtract my ones.



Now look at the tens, can I take away 8 tens? I need to regroup 1 hundred for 10 tens.

Children draw the Base 10 equipment, or the place value counters to



Children can start their formal written method by partitioning the number into clear place value columns.

$$836 - 254 = 582$$

H	T	O
800	30	6
-200	50	4

500	80	2

The children then progress to formal written methods.

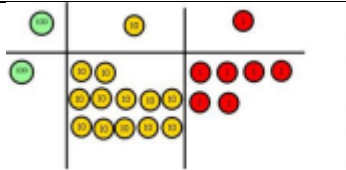
$$728 - 582$$

	H	T	O
	7	2	8
-	5	8	2

	1	4	6

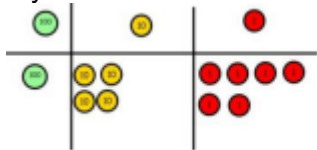
This will lead to subtracting any number

Progression in Calculations (2022/23)



$$\begin{array}{r} \text{Calculations} \\ 234 \\ - 88 \\ \hline \end{array}$$

Now I can take away 8 tens and complete my subtraction.



$$\begin{array}{r} \text{Calculations} \\ 234 \\ - 88 \\ \hline 146 \end{array}$$

Show how the concrete method links to the written method alongside your workings. Cross out the numbers when regrouping and show where and how we write the new amount.

$$\begin{array}{r} 234 \\ - 1562 \\ \hline 1192 \end{array}$$

including decimals

Use zeros for place holders.

$$\begin{array}{r} \\ \\ - \\ \hline \end{array}$$

$$\begin{array}{r} 106.99 \\ - 89.949 \\ \hline 60.750 \end{array}$$

$$\begin{array}{r} 15.49 \text{ kg} \\ - 36.080 \text{ kg} \\ \hline 69.339 \text{ kg} \end{array}$$




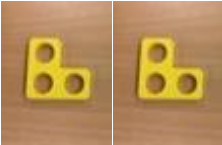
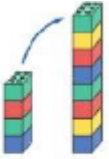

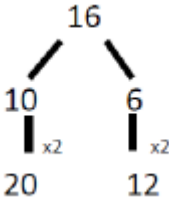


Progression in Calculations (2022/23)

Multiplication Vocabulary

Year R	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Double Equal groups Same	Repeated Addition Groups of Array Fact families Related facts Subitize	Times Multiple Lots of Multiplied by Inverse	Column multiplication	Product	Factor Common multiples Prime numbers Square numbers Composite numbers Cubed numbers Scaling	BODMAS Powers

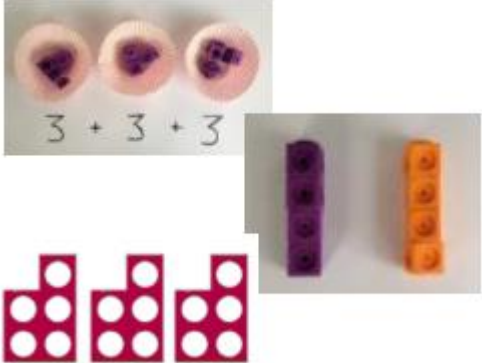
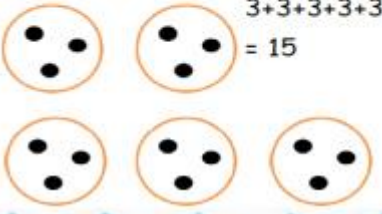
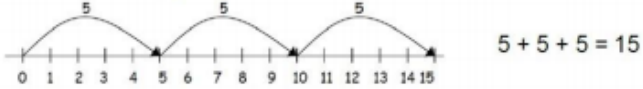

Multiplication Progression

Objectives and strategies	Concrete	Pictorial	Abstract
<p>Problem solving - doubling</p>	 <p>I have 3 pears. Can you double the number of pears?</p> 	 <p>Can you double the numicon shape?</p> 	<p>What is double 3?</p> <p>Double 3 is <input type="text"/></p>
<p>Doubling</p>	<p>Use practical activities to show how to double a number.</p>  <p>double 4 is 8 $4 \times 2 = 8$</p> <p>Model doubling using the Base ten equipment:</p> <p>Double 26 =</p>	<p>Draw pictures to show how to double a number.</p> <p>Double 4 is 8</p> 	<p>Partition a number and then double each part before recombining it back together.</p> 

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	<p>$40 + 12 = 52$</p>		
<p>Counting in multiples</p>	<p>Count in multiples supported by concrete objects in equal groups</p>	<p>Children make representations to show counting in multiples.</p>	<p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>2, 4, 6, 8, 10</p> <p>5, 10, 15, 20, 25, 30</p>

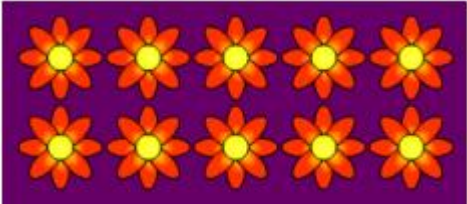
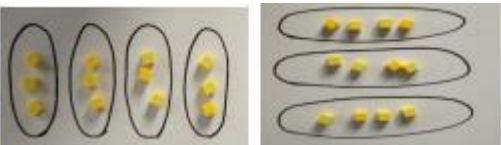
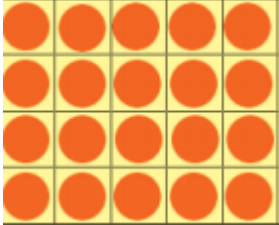

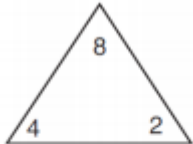
Progression in Calculations (2022/23)

<p>Repeated addition</p>	<p>Use different objects to add equal groups</p> 	<p>Use pictorial including number lines to solve problem</p> <p>There are 3 sweets in one bag. How many sweets are in 5 bags altogether?</p>  	<p>Write addition asences to describe objects and pictures.</p> 
<p>Counting in multiples from 0 (repeated addition)</p>	<p>Count the groups as children skip count. Use bar models.</p>	<p>Number lines, counting sticks and bar models should be used to show representation of counting in multiples.</p>	<p>Count in multiples of a number aloud. Write sequences with multiples of numbers.</p>

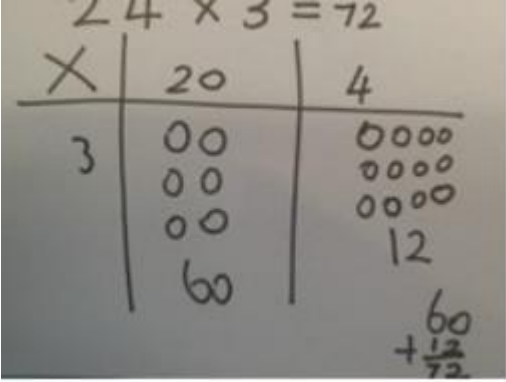
Progression in Calculations (2022/23)

	<p>$5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40$</p>		<p>0, 2, 4, 6, 8, 10 0, 3, 6, 9, 12, 15 0, 5, 10, 15, 20, 25, 30</p> <p>$4 \times 3 = \square$</p>
<p>Arrays showing commutative multiplication</p>	<p>Create arrays using counters/cubes to show multiplication sentences</p>	<p>Draw arrays in different rotations to find commutative multiplication sentences</p> <p>Link arrays to areas of rectangles.</p>	<p>Use an array to write multiplication sentences and reinforce repeated addition.</p> <p>$5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$</p>

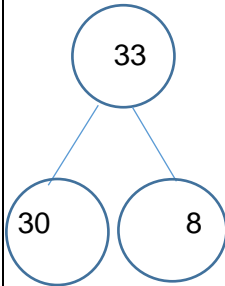
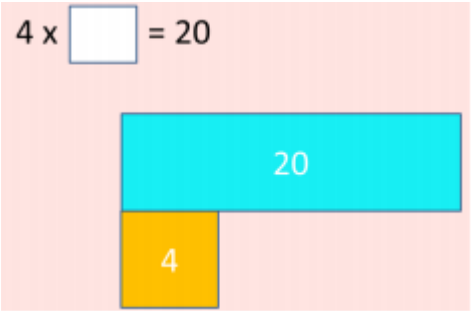
Progression in Calculations (2022/23)

	<p>And find answers to 2 lots of 5, 3 lots of 2 etc.</p>  <p>Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.</p> 		
<p>Using the inverse.</p> <p>This should be taught alongside division so pupils learn how they work</p>		<p>Fact Family</p>  $\square \times \square = \square$ $\square \times \square = \square$ $\square \div \square = \square$ $\square \div \square = \square$	<p>Show all 8 related fact family sentences.</p>

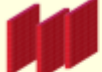











Progression in Calculations (2022/23)

<p>alongside each other.</p>			$2 \times 4 = 8$ $4 \times 2 = 8$ $8 \div 2 = 4$ $8 \div 4 = 2$ $8 = 2 \times 4$ $8 = 4 \times 2$ $2 = 8 \div 4$ $4 = 8 \div 2$															
<p>Partitioning</p>	<p>Use base ten to move towards a more compact method.</p> <p>$4 \times 13 =$</p> <table border="1" data-bbox="392 954 667 1098"> <thead> <tr> <th>x</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td></td> <td>40</td> <td>12</td> </tr> <tr> <td></td> <td>40</td> <td>12</td> </tr> <tr> <td></td> <td>40</td> <td>12</td> </tr> <tr> <td></td> <td>40</td> <td>12</td> </tr> </tbody> </table>	x	T	O		40	12		40	12		40	12		40	12	<p>Children can represent their work with place value counters in a way that they understand. They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking:</p> 	<p>Children use partitioning and use the multiplication facts that they know to help them by making numbers 10 x smaller to multiply then make them 10 x bigger in the answer.</p> <p>$33 \times 8 =$</p> <p>$30 \times 8 = 240$ $3 \times 8 = 24$</p> <p>$240 + 24 = 264$</p>
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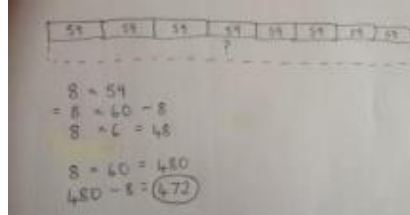
Progression in Calculations (2022/23)

		<p>Draw part whole models</p>  <p>Bar models are used to explore missing numbers</p> 	
<p>Column multiplication</p>	<p>Children continue to be supported by base ten equipment. This is initially done where there is no regrouping ie $321 \times 2 =$</p> <p>Progressing to re-grouping always multiply the ones column first. The corresponding long multiplication is modelled alongside.</p>	<p>Bar models and number lines can support learners when solving problems with multiplication</p>	<p>Start with long multiplication, reminding children about lining up their numbers clearly in columns.</p> <p>Initially, Children to write out what they are solving next to their answer to help them understand the process.</p>

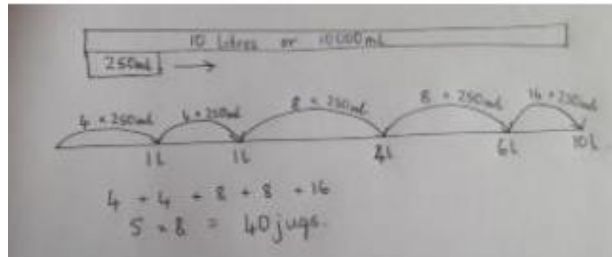
Progression in Calculations (2022/23)

Hundreds	Tens	Ones
		
		
		
		

alongside the formal written methods.

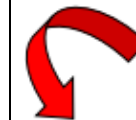


$8 = 54$
 $= 8 = 60 - 6$
 $8 = 66 - 12$
 $8 = 60 = 480$
 $480 - 8 = 472$



$$\begin{array}{r}
 32 \\
 \times 24 \\
 \hline
 8 \quad (4 \times 2) \\
 120 \quad (4 \times 30) \\
 40 \quad (20 \times 2) \\
 \hline
 600 \quad (20 \times 30) \\
 \hline
 768
 \end{array}$$

$$\begin{array}{r}
 327 \\
 \times 4 \\
 \hline
 28 \\
 80 \\
 \hline
 1200 \\
 1308
 \end{array}$$



	3	2	7
x			4
	1	3	0
			8
	1	2	

This may lead to a compact method.



Progression in Calculations (2022/23)

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Progression in Calculations (2022/23)

			$\begin{array}{r} 319 \\ \times 8 \\ \hline 2552 \end{array}$
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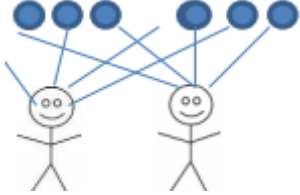
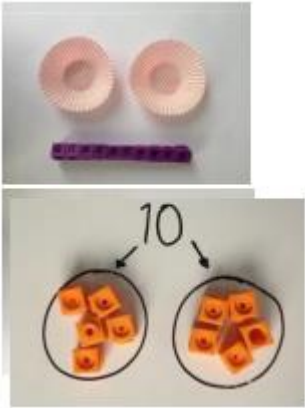

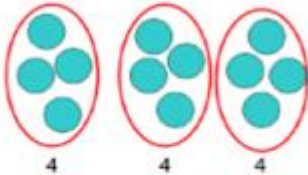
Division Vocabulary

Year R	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Share Half Equal Same	Groups Equal groups Unequal groups Less Division Divide Subitise	Left over Remainder Divide by Division	Shared equally between Divisible by Can be divided by	Short division	Divisibility rules	Remainders as decimals Remainders as fractions Divisor Dividend Quotient Annexing Ratio Scaling

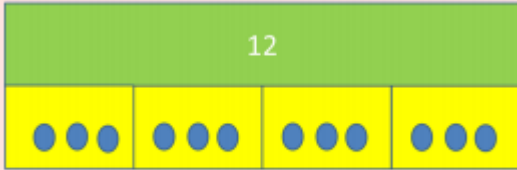

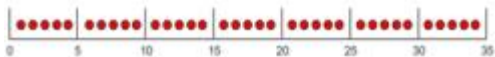
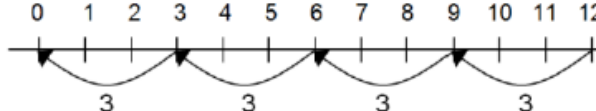
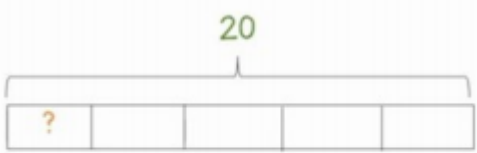
Division progression

Objectives and strategies	Concrete	Pictorial	Abstract
<p>Problem solving - halving</p>	 <p>I have 4 pencils. I give half of these pencils to a friend.</p> <p>Can you cut the cake/pizza in half?</p>	 <p>Cross off half of the holes on the Numicon. How many holes are left?</p>	<p>Half of 8 is <input type="text"/></p> <p>What is half of 8?</p>



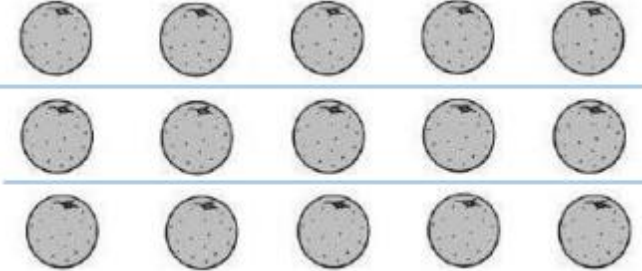
Progression in Calculations (2022/23)

<p>Problem solving - sharing</p>	 <p>Share these 6 beads between 3 children in the class.</p>	<p>Show how these marbles can be shared between two children</p> 	<p>What is 8 shared between 2?</p> <p>Ben has eight marbles and he wants to share them equally with his friend, Sam. How many marbles to they get each?</p>
<p>Sharing objects into groups</p>	<p>I have 10 cubes. Can you share them equally into 2 groups?</p> 	<p>Children use pictures or shapes to share quantities.</p>  <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $8 \div 2 = 4$ </div> <p>Sharing:</p>  <p style="color: red;">12 shared between 3 is 4</p>	<p>Share 9 sweets between 3 children</p> $9 \div 3 = 3$

Progression in Calculations (2022/23)

		<p>Children use bar modelling to show and support understanding.</p>  <p>$12 \div 4 = 3$</p>	
<p>Division as grouping</p>	<p>Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.</p>  	<p>Use a number line to show jumps in groups. The number of jumps equals the number of groups.</p>  <p>Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.</p>  <p>$20 \div 5 = ?$ $5 \times ? = 20$</p>	<p>$28 \div 7 = 4$</p> <p>Divide 28 into 7 groups. How many are in each group?</p>

Progression in Calculations (2022/23)

	<p>Use the Base Ten equipment or place value counters:</p> <p>24 divided into groups of 6 = 4</p> <p>$96 \div 3 = 32$</p> 		
<p>Division with arrays.</p>	<p>Link division to multiplication by creating an array and thinking about the number sentences that can be created.</p>  <p>Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$</p>	<p>Draw an array and use lines to split the array into groups to make multiplication and division sentences.</p> 	<p>Find the inverse of multiplication and division sentences by creating four linking family number sentences.</p> <p>$7 \times 4 = 28$ $4 \times 7 = 28$ $28 \div 7 = 4$ $28 \div 4 = 7$</p>

Progression in Calculations (2022/23)

Short division



Use place value counters to divide using the bus stop method alongside



Calculations
 $42 \div 3$

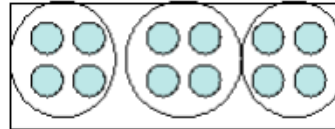


$42 \div 3 =$

Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.



Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



Encourage them to move towards counting in multiples to divide more efficiently.

Begin with divisions that divide equally with no remainder.

$$\begin{array}{r} 218 \\ 4 \overline{) 872} \\ \underline{8} \\ 7 \\ \underline{ 6} \\ 12 \\ \underline{ 12} \\ 0 \end{array}$$

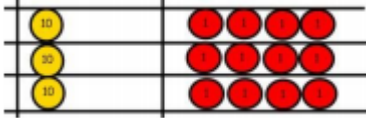
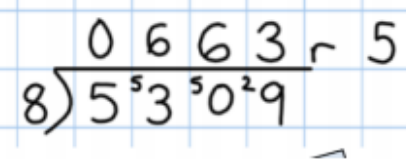

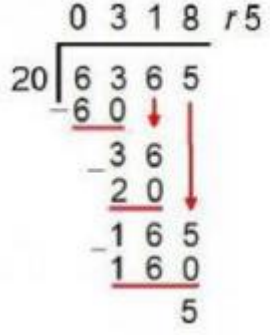
Move onto divisions with a remainder.

$$\begin{array}{r} 86 \text{ r } 2 \\ 5 \overline{) 432} \\ \underline{4} \\ 3 \\ \underline{ 2} \\ 12 \\ \underline{ 10} \\ 2 \end{array}$$

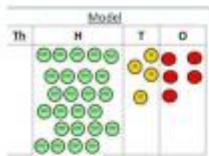
Move onto divisions with remainders expressed as fractions.

Finally move into decimal places to divide the total accurately for appropriate contexts.

Progression in Calculations (2022/23)

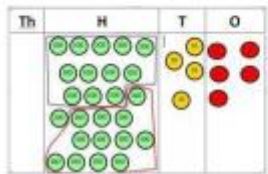
	<p>We regroup this ten for ten ones and then share the ones equally among the groups.</p>  <p>We look how much is in 1 group so the answer is 14.</p>		$\begin{array}{r} 14.6 \\ 35 \overline{) 511.0} \\ \underline{35} \\ 16 \\ \underline{15} \\ 10 \\ \underline{10} \\ 0 \end{array}$ 
<p>Long Division</p>	 <p>2544 ÷ 12 How many groups of 12 thousands do we have? None</p> <p>Regroup 2 thousands for 20 hundreds.</p>	<p>Instead of using physical counters, students can draw the counters and circle the groups on a whiteboard or in their books.</p> <p>Use this method to explain what is happening and as soon as they have understood what move on to the abstract method as this can be a time consuming process.</p>	

Progression in Calculations (2022/23)



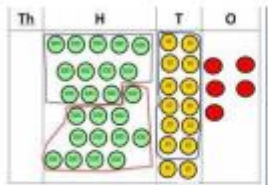
$$12 \overline{) 2544}^0$$

How many groups of 12 are in 25 hundreds? 2 groups. Circle them. We have grouped 24 hundreds so can take them off and we are left with one.



$$12 \overline{) 2544}^{02} \\ \underline{24} \\ 1$$

Regroup the 1 hundred for 10 tens so now we have 14 tens. How many groups of 12 are there in 14? 1 remainder 2.



$$12 \overline{) 2544}^{021} \\ \underline{24} \\ 14 \\ \underline{12} \\ 2$$

Regroup the 2 tens for 20 ones so now we have 24 ones. How many groups of 12 are in 24? 2

Express remainders as fractions

Express remainders as decimals

$432 \div 15$ becomes

$$15 \overline{) 432.0}^{28.8} \\ \underline{30} \quad \downarrow \\ 132 \\ \underline{120} \quad \downarrow \\ 120 \\ \underline{120} \\ 0$$

Answer: 28.8



Progression in Calculations (2022/23)

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